

1)  $81^{3/2}$  ← power  
                    ← ROOT

$$9^3 = 729$$

8)  $h^{-1}(x)$

$$h(x) = x^2 + 4$$

$$y = x^2 + 4$$

$$x = y^2 + 4$$

$$x - 4 = y^2$$

$$\pm \sqrt{x-4} = y$$

10)

## Section 10.1

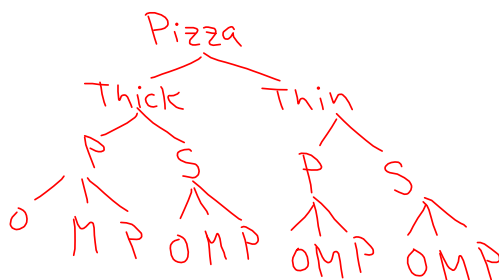
Fundamental counting principle:  $m \cdot n \cdot p$

different possible outcomes where  $m$ ,  $n$ ,  $p$  are separate events.

Small amounts you can use a tree diagram

How many combinations of pizza are possible? 12 Pizza

Given: thin or thick crust  
pepperoni or sausage  
olives, mushrooms or pineapple



What if the problem is too big to draw a tree diagram?

How many ways can you frame a picture?

Given: 12 frame styles  
55 colors for styles  
11 shades of blue mat

$$\underline{12} \cdot \underline{55} \cdot \underline{11} = 7,260$$

Frame color Mat

## License Plates

3 letters followed by 3 digits

Repeat:  $\frac{26}{L} \cdot \frac{26}{L} \cdot \frac{26}{L} \cdot \frac{10}{D} \cdot \frac{10}{D} \cdot \frac{10}{D}$   
 17,576,000

No Repeats:  $26 \cdot 25 \cdot 24 \cdot 10 \cdot 9 \cdot 8$   
 11,232,000

Number or letter:

R:  $\underline{36} \cdot \underline{36} \cdot \underline{36} \cdot \underline{36} \cdot \underline{36} \cdot \underline{36}$   $36^6 = 2,176,782,336$

No Repeat  $36^7 = 7.8 \text{ E}^{10}$   
 $36^8 = 2.82 \text{ E}^{12}$

## Permutation: Order matters

$${}_nP_r = \frac{n!}{(n-r)!}$$

$r$  = # choosing  
 $n$  = total

Factorials

$0! = 1$  by definition

$1! = 1$

$2! = 2 \cdot 1 = 2$

$3! = 3 \cdot 2 \cdot 1 = 6$

$4! = 4 \cdot 3 \cdot 2 \cdot 1 = 24$

Calculate:

$${}_5P_3 = \frac{5!}{(5-3)!} = \frac{5!}{2!} = 60$$

What would  $12!$  equal?

$$12 \cdot 11 \cdot 10 \cdot 9 \cdot 8 \cdot 7 \cdot 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 = 479,001,600$$

$${}_{24}P_5 = 5,100,480$$

How many ways can you burn 4 of 12 songs onto a CD?

$$P(12, 4)$$

$${}_{12}P_4$$

11,880

How many ways can you select a President, VP and secretary from a group of 10 people?

$${}_{10}P_3 = 720$$

## Distinguishable Permutations

How many ways to write

~~EYE~~  
 E E Y  
~~E E Y~~  
 Y E E

$$\frac{3!}{2!} = 3$$

|

~~MIAMI~~

$$\frac{(5!)}{(2!2!)} = 30$$

|

~~MISSISSIPPI~~  
 34,650

$$\frac{11!}{4!4!2!}$$

