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6.1 \& 6.2 Law of sines and cosines applications

Period $\qquad$ Date $\qquad$

1. Observers 2.32 mi apart see a hot-air balloon directly between them but at the angles of elevation shown in the figure. Find the altitude of the balloon.

2. A triangular field has sides of lengths 22, 36, 44 yd. Find the largest angle.
3. A boy is flying two kites at the same time. He has 380 ft of line out to one kite and 420 ft to the other. He estimates the angle between the two lines to be $30^{\circ}$. Approximate the distance between the kites.
4. A boat is cruising the ocean off a straight shore line. Points A and B are 120 mi apart on the shore. It is found that angles from the points to the boat are $42.3^{\circ}$ and $68.9^{\circ}$ respectively. Find the shortest distance from the boat to the shore.
5. Find the area of a regular octagon (8 equal sides, 8 equal angles) inscribed inside a circle of radius 9 inches.

6. Because deer require food, water, cover for protection from weather and predators and living space for healthy survival, there are natural limits to the number of deer that a given plot of land can support. Deer population in national parks average 14 animals per square kilometer. If a triangular region with side of 3 kilometers, 4 kilometers, and 6 kilometers has a population of 50 deer, how close is the population on this land to the average national park population?
7. 

multiple representations You are fertilizing a triangular garden. One side of the garden is 62 feet long and another side is 54 feet long. The angle opposite the 62 foot side is $58^{\circ}$.
a. Drawing a Diagram Draw a diagram to represent this situation.
b. Solving a Triangle Use the law of sines to solve the triangle you drew in part (a).
c. Applying a Formula One bag of fertilizer covers an area of 200 square feet. How many bags of fertilizer will you need to cover the entire garden?
8. Two markers A and B on the same side of a canyon rim are 80 ft apart, as shown in the figure. A hiker is located across the rim at point $C$. A surveyor determines that $\angle B A C=70^{\circ}$ and $\angle A B C=65^{\circ}$.
a) What is the distance between the hiker and point $A$ ?
b) What is the distance between the two canyon rims? (Assume they are parallel)

9. A pilot sets out from an airport and heads in the direction of $\mathrm{N} 20^{\circ} \mathrm{E}$, flying at 200 mph . After one hour, he makes a course correction and heads in the direction of $N 40^{\circ} \mathrm{E}$. Half an hour after that, engine trouble forces him to make an emergency landing.
a) Find the distance between the airport and his final landing point.
b) Find the bearing from the airport to his final landing.
10. A fisherman leaves his home port and heads in the direction of $\mathrm{N} 70^{\circ} \mathrm{W}$. He travels 30 miles and reaches Egg Island. The next day he sails $\mathrm{N} 10^{\circ} \mathrm{E}$ for 50 mi , reaching Forrest Island.
a) Find the distance between the fisherman's home port and Forrest Island.
b) Find the bearing from Forrest Island back to his home port.
11. Flights 104 and 217 are both approaching 0'Hare International Airport from directions directly opposite one another and at an altitude of 2.5 miles. The pilot on flight 104 reports an angle of depression of $170^{\circ} 4$ ' to the tower, and the pilot on flight 217 reports an angle of depression of $12^{\circ} 39^{\prime}$ to the tower. Calculate the distance between the planes.
12. A real estate agent has just take a trigonometry class at the local community college. She is considering purchasing a piece of property and is waiting for the surveyor's report before closing the deal. If the surveyor submits a drawing as in the figure below, explain why the agent will reject the sale.

13. The surveyor admits to his mistake and revises his drawing as in the next figure. This time the real estate agent refuses to complete the deal until additional information is supplied. What additional information is the real estate agent looking for to complete her knowledge about the parcel of land?

14. A portion of a barn, in the shape of an isosceles triangle, must be painted. The base of the triangle measures 30 feet long and the legs measure 20 feet each. A can of weatherproofing paint will cover 50 square feet of area. What is the minimum number of cans needed to cover this triangular portion? Show your work.

