

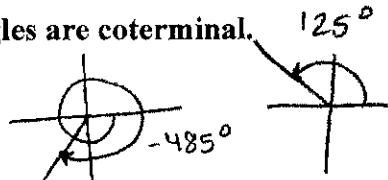
Review for Final #30

Date _____ Period _____

State if the given angles are coterminal.

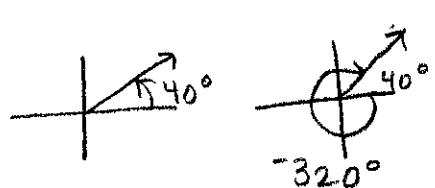
1) $125^\circ, -485^\circ$

NO



2) $40^\circ, -320^\circ$

yes



Find a positive and a negative coterminal angle for each given angle.

3) -165°

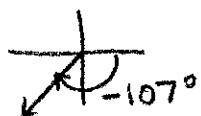
$$\begin{array}{r} -165^\circ \\ +360 \\ \hline 195^\circ \end{array}$$

$$\begin{array}{r} -165^\circ \\ -360 \\ \hline 525^\circ \end{array}$$

State the quadrant in which the terminal side of each angle lies.

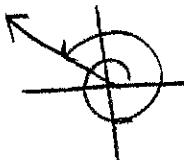
4) -107°

III



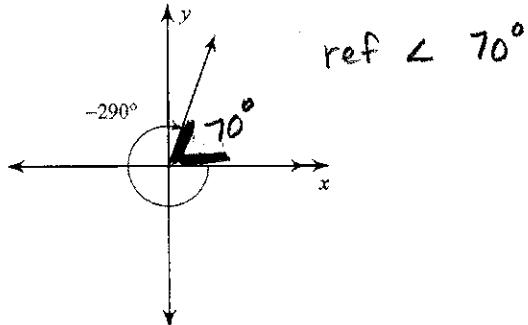
5) 520°

II

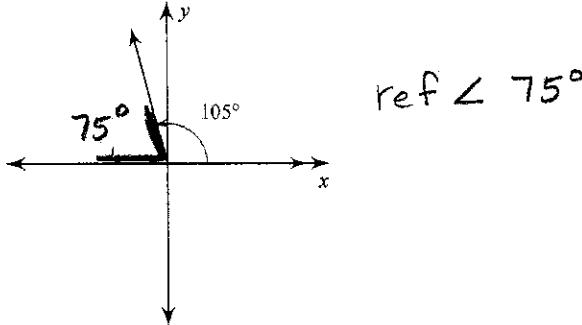


Find the reference angle.

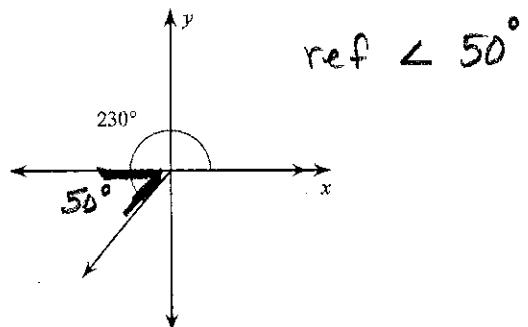
6)



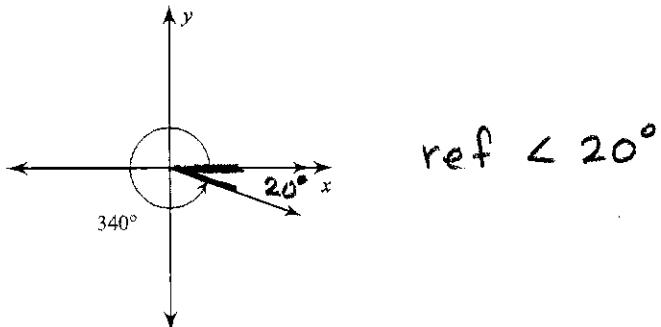
7)



8)



9)



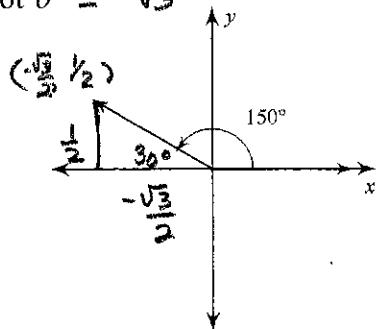
Convert each degree measure into radians and each radian measure into degrees.

10) $-285^\circ \left(\frac{\pi}{180^\circ} \right) = -\frac{19\pi}{12}$

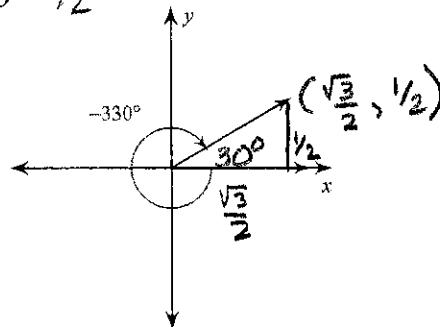
11) $\frac{17\pi}{9} \left(\frac{180^\circ}{\pi} \right) = 340^\circ$

Use your unit circle and find the exact value of each trigonometric function.

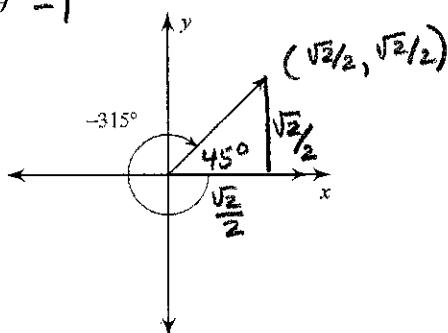
12) $\cot \theta = -\sqrt{3}$



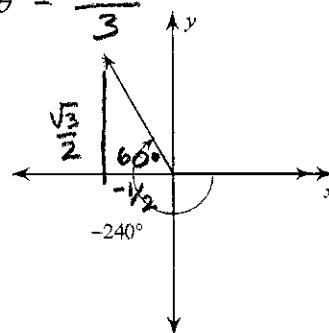
13) $\sin \theta = \frac{1}{2}$



14) $\tan \theta = 1$



15) $\csc \theta = \frac{2\sqrt{3}}{3}$



$$\frac{1}{\frac{\sqrt{3}}{2}} = \frac{2}{\sqrt{3}}$$

16) $\tan 330^\circ = -\sqrt{3}/3$

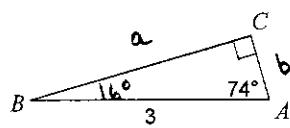
17) $\sin 360^\circ = 0$

18) $\cos(-135^\circ) = -\frac{\sqrt{2}}{2}$

19) $\tan \pi = 0$

Solve each triangle. Round answers to the nearest tenth.

20)



$$\sin 74^\circ = \frac{a}{3}$$

$$a = 2.88$$

$$\cos 74^\circ = \frac{b}{3}$$

$$b = .83$$

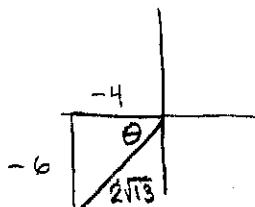
21) Given the following point. Graph and find all six trigonometric functions. State the reference angle.
(-4, -6)

$$\tan \theta = \frac{-6}{-4} = \frac{3}{2}$$

$$\theta = \tan^{-1}(-6/-4)$$

$$\theta = 56.3^\circ$$

$$\text{ref } \angle = 56.3^\circ$$



$$h^2 = (-4)^2 + (-6)^2$$

$$h = \sqrt{52} = 2\sqrt{13}$$

$$\sin \theta = \frac{-6}{2\sqrt{13}} = \frac{-3\sqrt{13}}{13}$$

$$\cos \theta = \frac{-4}{2\sqrt{13}} = \frac{-2\sqrt{13}}{13}$$

$$\tan \theta = -6/-4 = 3/2$$

$$\csc \theta = -\sqrt{13}/3$$

$$\sec \theta = -\sqrt{13}/2$$

$$\cot \theta = 2/3$$

Find the length of each arc.

22)

$$S = r\theta$$

$$S = 3(2\pi/3)$$

$$S = 2\pi \text{ yd}$$

$$\approx 6.28 \text{ yd}$$

23)

$$\text{Arc length} = \frac{135^\circ}{360^\circ} (2\pi(7))$$

$$= \frac{3}{8}(14\pi)$$

$$= \frac{21\pi}{4} \text{ in}$$

$$\approx 16.49 \text{ in.}$$

Find the area of each sector.

24)

$$A = \frac{315^\circ}{360^\circ} (\pi(18)^2)$$

$$A = \frac{567\pi}{2} \text{ cm}^2$$

$$\approx 890.64 \text{ cm}^2$$

25)

$$A = \frac{1}{2}r^2\theta$$

$$A = \frac{1}{2}(9)^2(4\pi/3)$$

$$A = 54\pi \text{ in}^2$$

$$\approx 169.64 \text{ in}^2$$

Using radians, find the amplitude and period of each function.

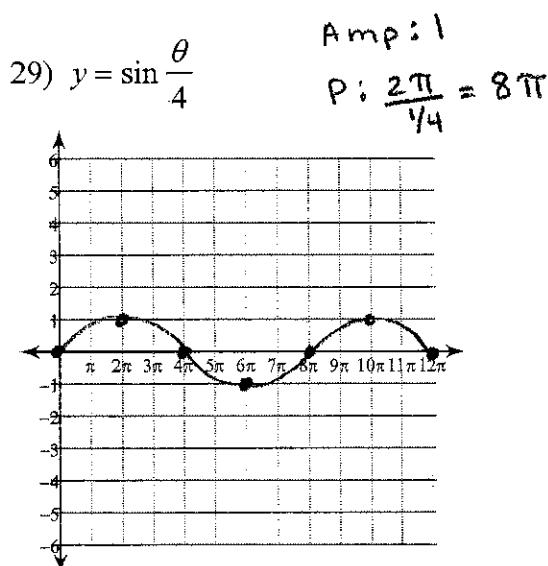
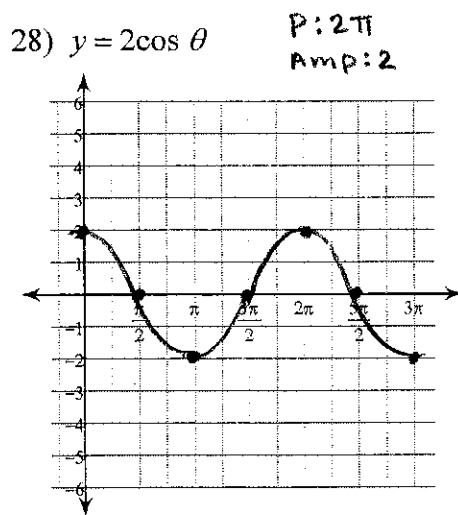
26) $y = 2\sin\left(\theta + \frac{7\pi}{4}\right)$

Amp: 2
period: $\frac{2\pi}{b} = \frac{2\pi}{1} = 2\pi$

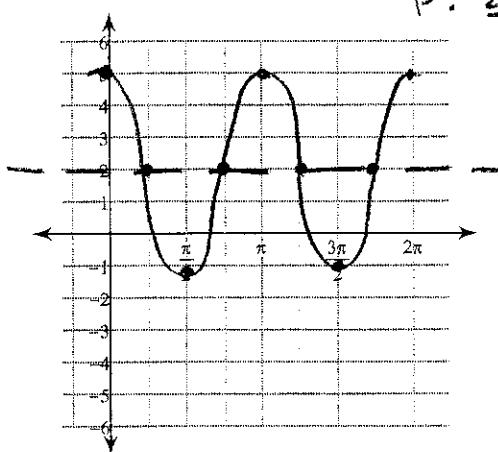
27) $y = 2 + 9\cos\left(\theta + \frac{7\pi}{6}\right)$

amp: 9
period: $\frac{2\pi}{b} = \frac{2\pi}{1} = 2\pi$

Graph each function using radians.



30) $y = 3\cos 2\theta + 2$

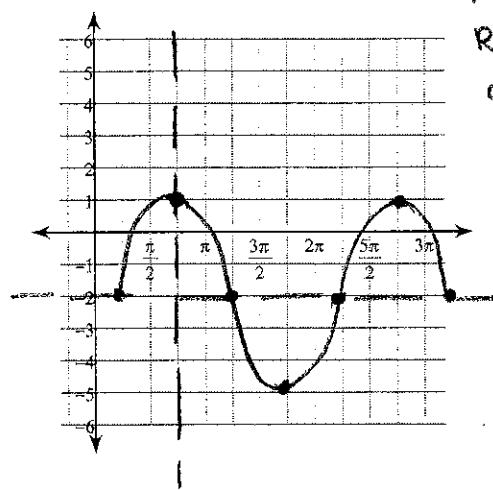


$$\text{Amp : } 3$$

$$P : \frac{2\pi}{2} = \pi$$

up 2.

32) $y = 3\cos\left(\theta - \frac{3\pi}{4}\right) - 2$



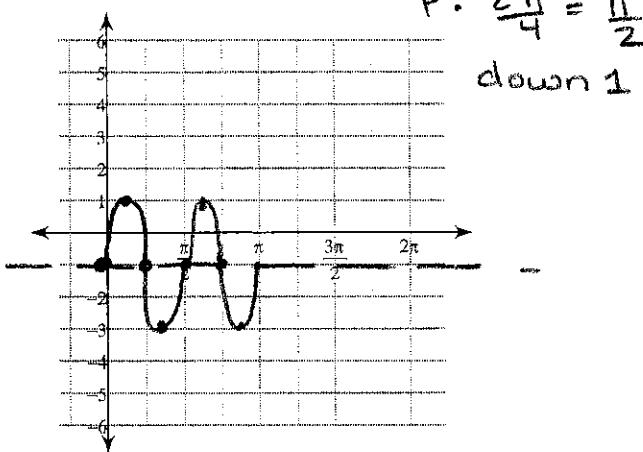
$$\text{amp: } 3$$

$$P: 2\pi$$

$$R: 3\pi/4$$

down 2

31) $y = -1 + 2\sin 4\theta$



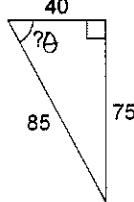
$$\text{amp: } 2$$

$$P: \frac{2\pi}{4} = \frac{\pi}{2}$$

down 1

Find the measure of the indicated angle to the nearest degree.

34)

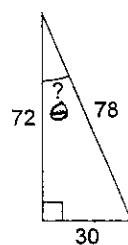


$$\tan \theta = \frac{75}{40}$$

$$\tan^{-1}\left(\frac{75}{40}\right) = \theta$$

$$\theta = 61.9^\circ$$

35)

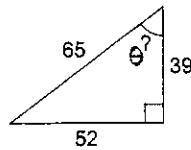


$$\sin \theta = \frac{30}{78}$$

$$\sin^{-1}\left(\frac{30}{78}\right) = \theta$$

$$\theta = 22.6^\circ$$

36)

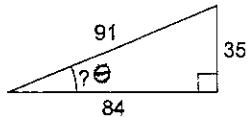


$$\cos \theta = \frac{39}{65}$$

$$\cos^{-1}\left(\frac{39}{65}\right) = \theta$$

$$\theta = 53.1^\circ$$

37)



$$\tan \theta = \frac{35}{84}$$

$$\tan^{-1}\left(\frac{35}{84}\right) = \theta$$

$$\theta = 22.6^\circ$$