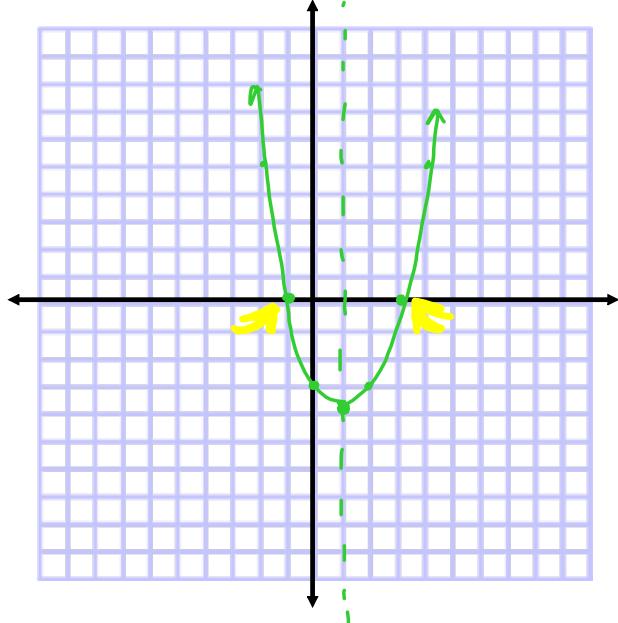


## Bellwork



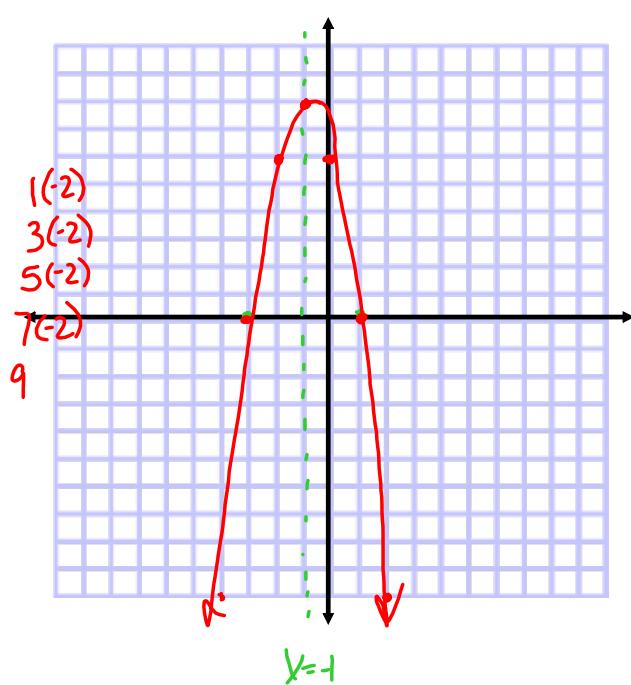
Graph  $y = x^2 - 2x - 3$   
 $x = \frac{-b}{2a} = 1$        $V: (1, -4)$

vertex form:  
 $y = (x-1)^2 - 4$

intercept form:  
 $y = (x+1)(x-3)$

Domain:  $(-1, 0) \cup (3, 0)$   
 $\mathbb{R}$

Range:  
 $[-4, \infty)$  interval  
 $y \geq -4$  inequality



Graph  $y = -2(x - 1)(x + 3)$   
 $-2(-1-1)(-1+3)$   
 $(1, 0) \cup (-3, 0)$

standard form:  
 $y = -2(x-1)(x+3)$

$y = -2(x^2 + 3x - x - 3) \Rightarrow y = -2x^2 - 4x + 6$

vertex form:  $V: (1, 8)$

$y = -2(x+1)^2 + 8$

x-intercept(s):  $(1, 0) \cup (-3, 0)$

y-intercept:  $(0, 6)$

## Quick review

Solve: factor / technique "square root both sides"

$$\frac{4(x-4)^2}{4} = \frac{24}{4}$$

$$\sqrt{(x-4)^2} = \sqrt{6}$$

$$x-4 = \pm\sqrt{6}$$

$$x = 4 \pm \sqrt{6}$$

$$x^2 - 8x - 20 = 0$$

$$\begin{array}{r} 1 \cdot 20 \\ 2 \cdot 10 \\ 4 \cdot 5 \end{array}$$

$$(x+2)(x-10) = 0$$

$$x = -2, 10$$

$$3(x+10)^2 - 21 = 0$$

$$3(x+10)^2 = 21$$

$$\sqrt{(x+10)^2} = \sqrt{7}$$

$$x+10 = \pm\sqrt{7}$$

$$x = -10 \pm \sqrt{7}$$

$$3x^2 - 13x = 10$$

$$3x^2 - 13x - 10 = 0$$

$$(3x+2)(x-5) = 0$$

$$x = -2/3, 5$$

What makes the following 2 expressions a perfect square trinomial?

$$\begin{array}{c} x^2 + 8x + 16 \\ \text{---} \\ (x+4)(x+4) \\ \text{---} \\ (x+4)^2 \end{array}$$

$$\begin{array}{c} x^2 + 12x + 36 \\ \text{---} \\ (x+6)(x+6) \\ \text{---} \\ (x+6)^2 \end{array}$$

Find the value of "c" that makes the expression a perfect square trinomial. Then write the expression as the square of a binomial.

$$\begin{array}{ll}
 x^2 + 10x + c & (\frac{10}{2})^2 = 25 \\
 (x+5)(x+5) & \left(\frac{b}{2}\right)^2 = \left(\frac{b}{2}\right)^2 \\
 (x+5)^2 & c'' = b^2/4 \\
 x^2 - 3x + c & \left(-\frac{3}{2}\right)^2 = \frac{9}{4} \\
 x^2 - 3x + \frac{9}{4} & (-\frac{3}{2})(\frac{3}{2}) = -\frac{9}{4} \\
 (x - \frac{3}{2})(x - \frac{3}{2}) & (\frac{b}{2})(\frac{b}{2}) = b^2/4 \\
 (x - \frac{3}{2})^2 & 
 \end{array}
 \quad
 \begin{array}{ll}
 x^2 - 14x + c & (\frac{-14}{2})^2 = 49 \\
 (x-7)(x-7) & (x-7)^2 \\
 (x-7)^2 & 
 \end{array}
 \quad
 \begin{array}{ll}
 x^2 + 5x + c & \left(\frac{5}{2}\right)^2 = \frac{25}{4} \\
 (x + \frac{5}{2})(x + \frac{5}{2}) & (\frac{5}{2})(\frac{5}{2}) = \frac{25}{4} \\
 (x + \frac{5}{2})^2 & 
 \end{array}$$

Solve by completing the square:

$$x^2 - 10x + 22 = 0 \quad \text{1) L.C. } 1x^2$$

$$x^2 + 12x - 54 = 0$$

$$x^2 + 12x + \underline{36} = 54 + \underline{36}$$

2) Separate ( $x$ 's 1 side  
 $\#$ 's other side)

$$\sqrt{(x+6)^2} = \sqrt{90}$$

$$x^2 - 10x + \frac{25}{\uparrow c} = -22 + \underline{25}$$

$$\sqrt{(x-5)^2} = \pm \sqrt{3}$$

$$x-5 = \pm \sqrt{3}$$

$$x = 5 \pm \sqrt{3}$$

3) Find " $c$ "  $(\frac{b}{2})^2$

4) Balance

5)  $(\quad )^2$

6) Solve

$$x+6 = \pm \sqrt{90}$$

$$x = -6 \pm \sqrt{90}$$

$$x = -6 \pm 3\sqrt{10}$$

$$x^2 - 8x = -8$$

$$\begin{aligned} x^2 - 8x + \underline{16} &= -8 + \underline{16} \\ \sqrt{(x-4)^2} &= \sqrt{8} \\ x-4 &= \pm \sqrt{8} \\ x &= 4 \pm 2\sqrt{2} \end{aligned}$$

$$2x^2 + 28x = -36$$

$$\begin{aligned} x^2 + 14x + \underline{49} &= -18 + \underline{49} \\ \sqrt{(x+7)^2} &= \sqrt{31} \\ x+7 &= \pm \sqrt{31} \\ x &= -7 \pm \sqrt{31} \\ 2(x^2 + 14x + \underline{49}) &= -36 + \underline{98} \\ 2(x+7)^2 &= 62 \\ (x+7)^2 &= 31 \\ x+7 &= \pm \sqrt{31} \\ x &= -7 \pm \sqrt{31} \end{aligned}$$

$$3x^2 - 12x + 4 = 0$$

$$\begin{aligned} 3x^2 - 12x &= -4 \\ 3(x^2 - 4x + \underline{4}) &= -4 + \underline{12} \end{aligned}$$

$$\begin{aligned} 3(x-2)^2 &= 8 \\ \sqrt{(x-2)^2} &= \sqrt{\frac{8}{3}} \\ x-2 &= \pm \frac{2\sqrt{2}\sqrt{3}}{\sqrt{3}\sqrt{3}} \\ x &= 2 \pm \frac{2\sqrt{6}}{3} \end{aligned}$$

$$5x^2 + 20x + 2 = 0$$

$$\begin{aligned} 5x^2 + 20x &= -2 \\ 5(x^2 + 4x + \underline{4}) &= -2 + \underline{20} \end{aligned}$$

$$\begin{aligned} 5(x+2)^2 &= 18 \\ (x+2)^2 &= \frac{18}{5} \end{aligned}$$

$$x+2 = \pm \sqrt{\frac{18}{5}}$$

$$x = -2 \pm \frac{3\sqrt{2}\sqrt{5}}{\sqrt{5}\sqrt{5}}$$

$$x = -2 \pm \frac{3\sqrt{10}}{5}$$

Write in vertex form by using completing the square method:

$$y = x^2 - 10x - 20 \quad (\quad )^2 + \underline{\quad} \quad y = 3x^2 - 6x + 1$$

$$y = x^2 - 10x + \frac{25}{\uparrow} - 20 + \frac{-25}{\uparrow} \quad y = 3x^2 - 6x + 1$$
$$y = (x-5)^2 - 45 \quad y = 3(x^2 - 2x + \underline{1}) + 1 + \underline{-1}$$

STOP  
vertex form

$$y = 3(x-1)^2$$

Stop

$$y = x^2 + 4x + 5$$

$$y = x^2 + 4x + \frac{4}{\uparrow} + 5 + \frac{-4}{\uparrow}$$
$$y = (x+2)^2 + 1$$

$$y = 3x^2 - 12x + 7$$

$$y = 3x^2 - 12x + 7$$
$$y = 3(x^2 - 4x + \frac{4}{\uparrow}) + 7 + \frac{-12}{\uparrow}$$

$$y = 3(x-2)^2 - 5$$

