

Precalculus  
Review 1.1-1.5

Name Key  
Period \_\_\_\_\_ Date \_\_\_\_\_

1. Graph:  $(x - 1)^2 + (y + 3)^2 = 9$       C: (1, -3)  
R: 3

2. Write the equation of the circle with the given information.

a) center: (-4, 7) and radius: 8

$$(x+4)^2 + (y-7)^2 = 64$$

b) endpoints of diameter: (-2, -5) and (-2, 9)

$$(x+2)^2 + (y-2)^2 = 49 \quad R: 7 \quad C: (-2, 2)$$

c) center (-1, -4) and solution point (4, 8)

$$(x+1)^2 + (y+4)^2 = r^2$$

$$(x+1)^2 + (y+4)^2 = 169$$

$$(4+1)^2 + (8+4)^2 = r^2$$

$$r = 13$$

3. Write the equation of the line with the given information.

a) Through the point (3, -5) with slope  $\frac{2}{3}$

$$y - -5 = \frac{2}{3}(x - 3)$$

$$3y + 15 = 2(x - 3)$$

$$3y = 2x - 21$$

$$y + 5 = \frac{2}{3}(x - 3)$$

$$3y + 15 = 2x - 6$$

$$y = \frac{2}{3}x - 7 \star$$

b) Through points (-3, -7) and (1, 6)

$$m = \frac{-7-6}{-3-1} = \frac{-13}{-4} = \frac{13}{4}$$

$$y - 6 = \frac{13}{4}(x - 1)$$

$$4y = 13x + 11$$

$$4y - 24 = 13x - 13$$

$$y = \frac{13}{4}x + \frac{11}{4} \star$$

c) Parallel to the line  $-4x + 16y = 10$  and passes through the point (-2, 9)

$$16y = 4x + 10$$

$$m = \frac{1}{4}$$

$$y = \frac{1}{4}x + \frac{10}{16}$$

$$y - 9 = \frac{1}{4}(x + 2)$$

$$y = \frac{1}{4}x + \frac{19}{2} \star$$

$$y = \frac{1}{4}x + \frac{5}{8}$$

$$y = \frac{1}{4}x + \frac{1}{2} + 9$$

d) Perpendicular to the line  $-4x + 16y = 10$  and passes through the point (-2, 9)

$$\perp m = -4$$

$$y - 9 = -4(x + 2)$$

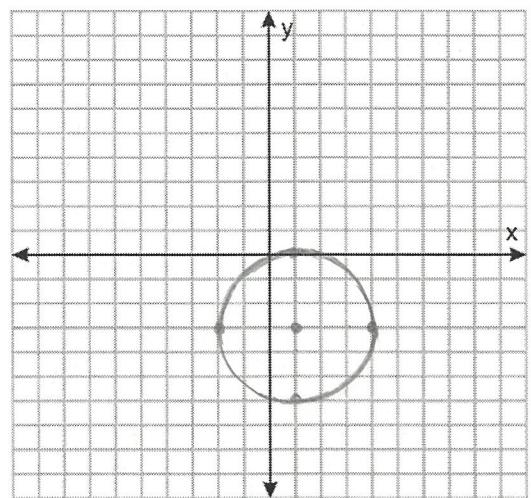
$$y = -4x + 1 \star$$

$$y = -4x - 8 + 9$$

e) Perpendicular to the line  $y = \frac{5}{7}x - 9$

$$\perp m = -\frac{7}{5}$$

$$y = -\frac{7}{5}x + \boxed{\phantom{0}}$$



4. Find the distance between the 2 points  $(-8, -1)$  and  $(-3, -6)$

$$d = \sqrt{(-8 + 3)^2 + (-1 + 6)^2}$$

$$d = \sqrt{50} = 5\sqrt{2} \approx 7.071$$

5. Find the slope between the 2 points  $(2, 4)$  and  $(8, -6)$

$$m = \frac{4 + 6}{2 - 8} = \frac{10}{-6} = -\frac{5}{3}$$

6. Solve for A. Given:  $m = \frac{2}{7}$  between the 2 points  $(A, 6)$  and  $(2, -4)$

$$\frac{2}{7} = \frac{6 + 4}{A - 2}$$

$$2A - 4 = 70$$

$$2A = 74$$

$$A = 37$$

7. Determine whether the function is odd, even or neither. Describe its symmetry.

a)  $f(x) = \frac{x^2 - 5}{4x}$      $\frac{(-x)^2 - 5}{4(-x)} = -\frac{x^2 - 5}{4x}$     odd  
symmetry origin

b)  $f(x) = 3x^3 - 9x^2 + 4x + 8$

$$3(-x)^3 - 9(-x)^2 + 4(-x) + 8$$

$$-3x^3 - 9x^2 - 4x + 8$$

Neither

c)  $g(x) = \frac{1}{x} - 4$

$$= \frac{1}{(-x)} - 4 \Rightarrow -\frac{1}{x} - 4$$

Neither

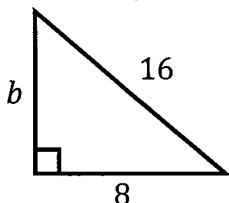
d)  $h(x) = x^4 - 16x^2$

$$= (-x)^4 - 16(-x)^2$$

$$= x^4 - 16x^2$$

even  
symmetry y-axis

8. Find the length of side  $b$ .



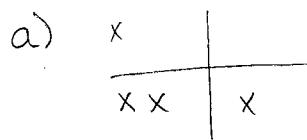
$$b = \sqrt{16^2 - 8^2}$$

$$b = 8\sqrt{3}$$

$$b \approx 13.856$$

9. Determine the quadrant(s) in which  $(x, y)$  could be located, given:

a)  $x = -5$  and  $y < 0$  III



b)  $x > 0$  and  $y > 0$  I



10. Find the  $y$ -intercept for the given function.

$$y = \frac{x+6}{|x-1|}$$

$$y = \frac{0+6}{|0-1|} = \frac{6}{1} = 6 \quad (0, 6)$$

11. Find the zeros.

$$f(x) = 7x^2 - 25x - 12$$

$$0 = (7x + 3)(x - 4)$$

$$x = -\frac{3}{7} \quad x = 4$$

12. Find the average rate of change from  $x_1$  to  $x_2$  for the given function  $(x) = x^3 - 2x^2 + 1$ .

a)  $x_1 = -2$  to  $x_2 = -3$

$$(-2, -15)$$

$$(-3, -44)$$

b)  $x_1 = 3$  to  $x_2 = 5$

$$(3, 10)$$

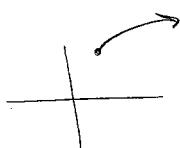
$$(5, 76)$$

$$m = \frac{-15 + 44}{-2 + 3} = \frac{29}{1} = 29$$

$$m = \frac{10 - 76}{3 - 5} = \frac{-66}{-2} = 33$$

13. Find the domain of the given functions.

a)  $f(x) = \sqrt{x-2} + 8$



$$D: [2, \infty) \text{ or } x \geq 2$$

b)  $g(x) = \frac{x^2+2x+4}{x+7}$   
 $x \neq -7$

$$D: \mathbb{R}, x \neq -7 \text{ or } (-\infty, -7) \cup (-7, \infty)$$

c)  $h(x) = \frac{\sqrt{x-5}}{x-9}$   
 $x \geq 5$   
 $x \neq 9$

$$D: x \geq 5, x \neq 9 \text{ or } [5, 9) \cup (9, \infty)$$

14. Find the maximum and minimum values of the given function.

$$f(x) = x^3 - 2x^2 - 2x + 8$$

$$\text{Max: } (-3.87, 8.416)$$

$$\text{Min: } (1.720, 3.731)$$

15. Find the  $x$  and  $y$  intercept(s).

a)  $x^4 - 4x^2 - 45$   
 $(x^2 - 9)(x^2 + 5)$   
 $(x+3)(x-3)(x^2+5)$

$$x\text{-int: } (-3, 0) (3, 0)$$

$$y\text{-int: } (0, -45)$$

b)  $x^2 + 12x - 64$   
 $(x+16)(x-4)$

$$x\text{-int: } (-16, 0) (4, 0)$$

$$y\text{-int: } (0, -64)$$

16. Given:  $f(x) = \begin{cases} -2x + 7, & x < -1 \\ (x-2)^2 - 3, & x \geq -1 \end{cases}$

a)  $f(-3) = -2(-3) + 7 = 13$

b)  $f(-1) = (-1-2)^2 - 3 = 6$

c)  $f(2) = (2-2)^2 - 3 = -3$

17. Determine the intervals over which the function is increasing, decreasing or constant.

constant  $(-6, -4)$

increase  $(-4, -1) \cup (4, \infty)$

decrease  $(-4, -3) \cup (-1, 4)$

