

Solve the systems algebraically.

<p>1. $y = x^2 + 18x + 35$ $y = -x^2 + 2x + 5$ $x^2 + 18x + 35 = -x^2 + 2x + 5$ $2x^2 + 16x + 30 = 0$ $2(x^2 + 8x + 15) = 0$ $(-5, -30)$ $2(x + 5)(x + 3) = 0$ $(-3, -10)$ $x = -5$ $x = -3$</p>	<p>2. $y = x^2 + 16x + 32$ $y = -x^2 + 2$ $x^2 + 16x + 32 = -x^2 + 2$ $(-5, -23)$ $2x^2 + 16x + 30 = 0$ $2(x^2 + 8x + 15) = 0$ $(-3, -7)$ $2(x + 5)(x + 3) = 0$ $x = -5$ $x = -3$</p>
<p>3. $y = x^2 + 16x + 32$ $y = -x^2 + 2$ Same as #2</p>	<p>4. $y = x^2 + 3x - 7$ $x + y = -2$ $y = -x - 2$ $-x - 2 = x^2 + 3x - 7$ $(-5, 3)$ $0 = x^2 + 4x - 5$ $0 = (x + 5)(x - 1)$ $(1, -3)$ $x = -5$ $x = 1$</p>

Solve the following quadratic functions.

<p>5. $-4x^2 - 7x = -3$ $4x^2 + 7x - 3 = 0$ $(\quad x \quad) = 0$ $x = \frac{-7 \pm \sqrt{49 - 4(4)(-3)}}{2(4)}$ $x = \frac{-7 \pm \sqrt{97}}{8}$</p>	<p>6. $x^2 + 10x + 18 = 0$ $x = \frac{-10 \pm \sqrt{100 - 4(1)(18)}}{2(1)}$ $x = \frac{-10 \pm \sqrt{28}}{2}$ $x = \frac{-10 \pm 2\sqrt{7}}{2}$ $x = -5 \pm \sqrt{7}$</p>
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Use the discriminant to determine the number of real solutions.

<p>7. $x^2 + 3x + 5 = 0$ $b^2 - 4ac$ discriminant $9 - 4(1)(5) =$ -11 2 imaginary solutions</p>	<p>8. $2x^2 + 2 = -4x$ $2x^2 + 4x + 2 = 0$ $b^2 - 4ac$ $16 - 4(2)(2)$ $16 - 16 = 0$ 1 real solution</p>
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Factor the polynomial completely.

9. $x^3 - 6x^2 - 72x$ $x(x^2 - 6x - 72)$ $x(x-12)(x+6)$	10. $3y^5 - 48y^3$ $3y^3(y^2 - 16)$ $3y^3(y+4)(y-4)$
11. $x^3 + 8$ $(x+2)(x^2 - 2x + 4)$	12. $x^3 + x^2 + x + 1$ $x^2(x+1) + 1(x+1)$ $(x+1)(x^2 + 1)$
13. $4x^3 + 8x^2 - 9x - 18$ $4x^2(x+2) - 9(x+2)$ $(x+2)(4x^2 - 9)$ $(x+2)(2x-3)(2x+3)$	14. $y^3 - 64$ $(y-4)(y^2 + 4y + 16)$
15. $x^4 - 25$ $(x^2 + 5)(x^2 - 5)$ $(x^2 + 5)(x + \sqrt{5})(x - \sqrt{5})$	16. $3x^4 - x^2 - 24$ $(3x^2 + 8)(x^2 - 3)$ $(3x^2 + 8)(x + \sqrt{3})(x - \sqrt{3})$

Write a polynomial function of least degree that has rational coefficients, a leading coefficient of 1 and the given zeros.

17. $x = 3, x = 2$ $(x-3)(x-2)$ $f(x) = x^2 - 5x + 6$	18. $x = \frac{1}{2}, x = -2$ $(x - \frac{1}{2})(x + 2)$ $f(x) = x^2 + 2x - \frac{1}{2}x - 1$ $f(x) = x^2 + \frac{3}{2}x - 1$
19. $x = \sqrt{5}, x = -\sqrt{5}$ $(x - \sqrt{5})(x + \sqrt{5})$ $f(x) = x^2 - 5$	20. $x = 3i, x = -3i$ $(x - 3i)(x + 3i)$ $x^2 - 9i^2$ $x^2 - 9(-1)$ $f(x) = x^2 + 9$
21. $x = 2 + i, x = 2 - i$ $(x - 2 - i)(x - 2 + i)$ $x^2 - 2x + xi$ $-2x \quad + 4 - 2i$ $\quad \quad -xi \quad + 2i - i^2$ $f(x) = x^2 - 4x + 5$	22. $x = \sqrt{7}, x = -\sqrt{7}$ $(x - \sqrt{7})(x + \sqrt{7})$ $x^2 - 7$ $f(x) = x^2 - 7$

Algebra 2
BLOCK 6 ASSESSMENT Student Copy
2009-10

1. Find the domain and range of:

$$y = 2\cos x$$

Domain: \mathbb{R}
Range: $[-2, 2]$
 $-2 \leq y \leq 2$

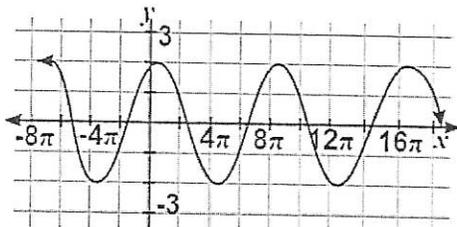
A) D: all real numbers
R: $2 \leq y \leq 6$

B) D: all real numbers
R: $-2\pi \leq x \leq 2\pi$,

C) D: $x \geq \frac{\pi}{3}$
R: $-3 \leq y \leq 3$

**D) D: all real numbers
R: $-2 \leq y \leq 2$**

2. Find the domain and range of the sin function graphed below:



A) D: $x \geq \frac{\pi}{6}$
R: $-2 \leq y \leq 2$

**B) D: all real numbers
R: $-2 \leq y \leq 2$**

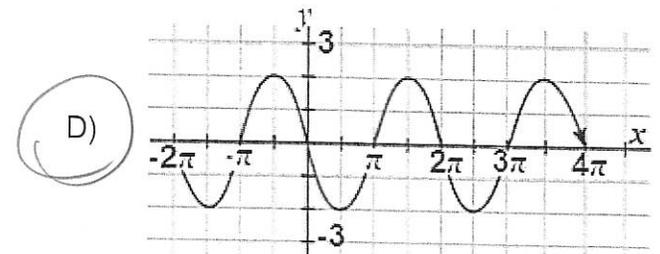
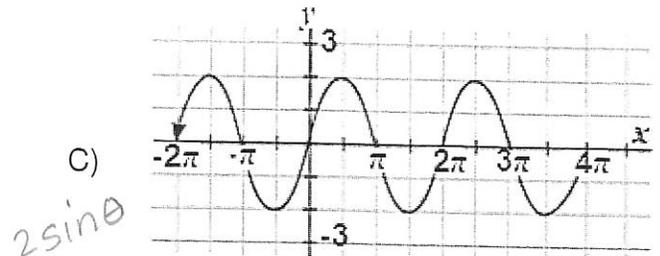
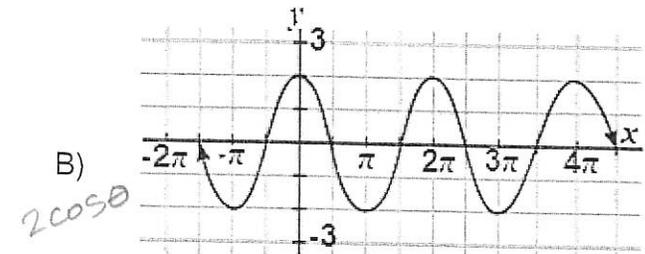
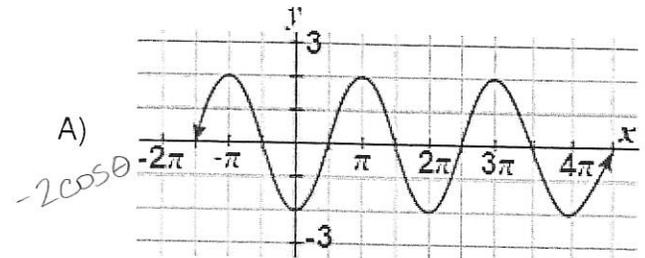
C) D: $x \leq \frac{\pi}{2}$
R: $-3 \leq y \leq 3$

D) D: all real numbers
R: $-1 \leq y \leq 3$

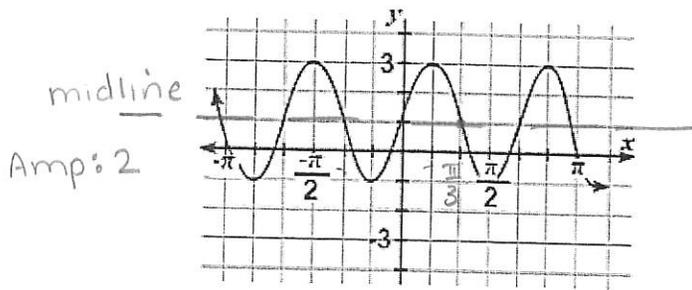
Domain: \mathbb{R}
Range: $[-2, 2]$
 $-2 \leq y \leq 2$

3. Determine which of these answers is the correct graph of the function shown here.

$$f(x) = -2\sin \theta$$

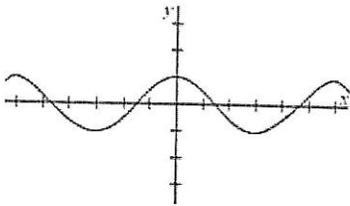


4. Determine which of these answers is the correct equation for the graph shown here.

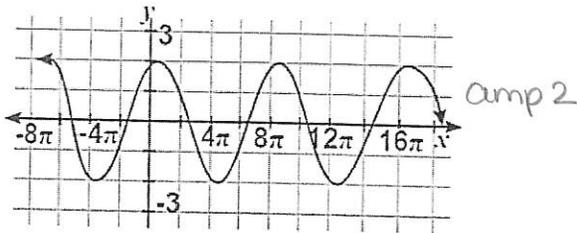


- A) $f(x) = 1 - 2\sin(3x + \pi)$ left $\pi/3$
 B) $f(x) = 1 + 2\sin(3(x - \pi))$ right π
 C) $f(x) = 1 - 2\cos(3(x + \pi))$ left π
 D) $f(x) = 1 + 2\cos(3x - \pi)$ right $\pi/3$

5.



Based on the parent function $f(x) = \cos x$ above, determine which of these answers is the correct equation for the graph shown here.



- A) $f(x) = 2\cos\frac{1}{4}(x - \pi)$ $P = \frac{2\pi}{1/4} = 8\pi$
~~B) $f(x) = 4\sin\frac{1}{2}(x + \pi)$ $P = \frac{2\pi}{1/2} = 4\pi$~~
 C) $f(x) = 2\sin\left(\frac{x}{4} - \pi\right)$ $P = 2\pi$
~~D) $f(x) = 4\cos 2(x + \pi)$ $P = \pi$~~

6. Change this fraction to its degree measure.

$$\frac{5\pi}{2} \left(\frac{180^\circ}{\pi} \right) = 450^\circ$$

- A) 550°
 B) 500°
 C) 450°
 D) 300°

7. Change -220° to its radian measure.

$$\text{A) } \frac{-11\pi}{9} \quad -220^\circ \left(\frac{\pi}{180^\circ} \right) = \frac{-11\pi}{9}$$

B) $\frac{9\pi}{11}$

C) $\frac{-9\pi}{11}$

D) $\frac{11\pi}{9}$

8. If $\tan \theta = -1$, for $\pi \leq \theta \leq 2\pi$, find the exact value for θ .

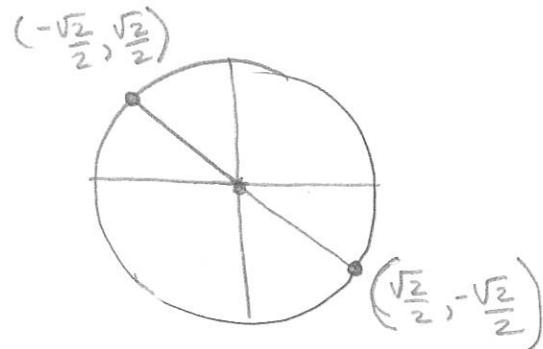
use unit circle

A) $\frac{7\pi}{4}$

B) $\frac{4\pi}{3}$

C) $\frac{5\pi}{4}$

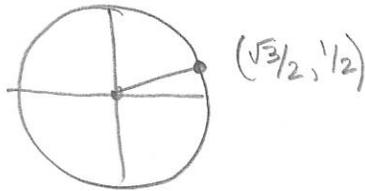
D) $\frac{5\pi}{3}$



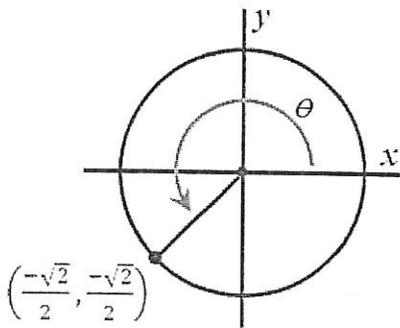
unit circle

9. If $\sin \theta = \frac{1}{2}$, for $0 \leq \theta \leq \frac{\pi}{2}$, then $\theta = ?$

- A) $\frac{\pi}{3}$
- B) $\frac{7\pi}{6}$
- C) $\frac{\pi}{6}$
- D) $\frac{5\pi}{3}$



10. Find $\tan \theta$, given the point on the unit circle pictured.

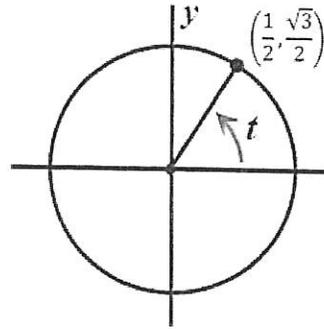


- A) $\frac{-\sqrt{3}}{2}$
- B) 0
- C) 1
- D) -1

$$\tan \theta = \frac{y}{x} = \frac{\text{opp}}{\text{adj}} = \frac{\sin \theta}{\cos \theta}$$

11. Find $\cos t$, given the point on the unit circle pictured.

$(\cos \theta, \sin \theta)$
 (x, y)



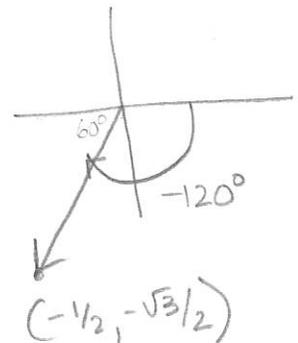
- A) $\frac{1}{2}$
- B) $\frac{-1}{2}$
- C) $\frac{-\sqrt{3}}{2}$
- D) $\frac{-\sqrt{2}}{2}$

12. Find the value of the function shown here:

$$\sin\left(\frac{-2}{3}\pi\right)$$

go to this angle
on unit circle
★ rotate clockwise

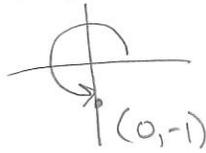
- A) $\frac{-1}{2}$
- B) $\frac{-\sqrt{2}}{2}$
- C) $\frac{-\sqrt{5}}{2}$
- D) $\frac{-\sqrt{3}}{2}$



unit circle

13. Find the value of $\tan\left(\frac{3\pi}{2}\right)$. 270°

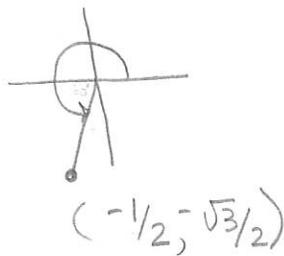
- A) 0
- B) $\sqrt{3}$
- C) Undefined
- D) -1



unit circle

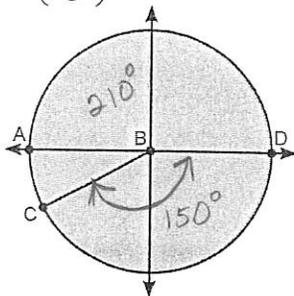
14. Find the value of $\cos\left(\frac{4\pi}{3}\right)$. 240°

- A) $\frac{\sqrt{2}}{2}$
- B) $-\frac{1}{2}$
- C) $\frac{1}{2}$
- D) $-\frac{\sqrt{3}}{2}$



15. Find the length of \widehat{DAC} given $\overline{BC} = 3$, and $\angle DBC = -\left(\frac{5\pi}{6}\right)$.

$210^\circ = \frac{7\pi}{6}$



- A) $\frac{5\pi}{2}$
- B) $\frac{21\pi}{2}$
- C) $\frac{7\pi}{2}$
- D) $\frac{15\pi}{2}$

arc length $s = r\theta$

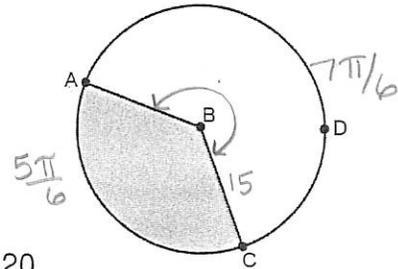
$S = 3\left(\frac{7\pi}{6}\right)$

$S = \frac{21\pi}{6}$

$S = \frac{7\pi}{2}$

measure

16. Given the length of $\widehat{ADC} = \frac{7\pi}{6}$, $r = 15$, find the area of the shaded sector in $\odot B$ using radian measure.



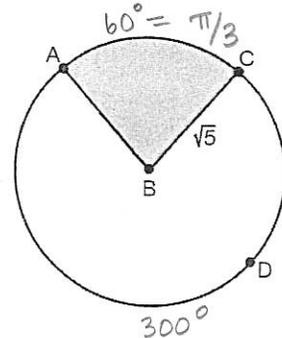
- A) 20
- B) $\frac{\pi}{18}$
- C) $\frac{4\pi}{3}$
- D) $\frac{375\pi}{4}$

$A = \frac{1}{2} r^2 \theta$

$A = \frac{1}{2} (15)^2 \left(\frac{5\pi}{6}\right)$

$A = \frac{375\pi}{4}$

17. Given $m\widehat{ADC} = \frac{5\pi}{3}$, $r = \sqrt{5}$, find the area of the shaded sector in $\odot B$ using radian measure.



- A) $\frac{5\pi}{6}$
- B) $\frac{11\pi}{6}$
- C) $\frac{13\pi}{6}$
- D) $\frac{\pi}{6}$

$A = \frac{1}{2} r^2 \theta$

$A = \frac{1}{2} (\sqrt{5})^2 \left(\frac{\pi}{3}\right)$

$A = \frac{5\pi}{6}$