

Honors Math II
Factoring

Name Key
Period _____ Date _____

Factor the following polynomials using synthetic/long division.

1. $x^3 - 2x^2 - 11x + 12$ if $(x - 1)$ is one of the factors.

$$\begin{array}{r} \boxed{1} & -2 & -11 & 12 \\ & 1 & -3 & -12 \\ \hline & 1 & -1 & -12 & 0 \end{array} \quad \begin{array}{l} x^2 - x - 12 \\ (x - 4)(x + 3) \end{array} \quad (x - 1)(x + 3)(x - 4)$$

2. $x^3 + x^2 - 4x - 4$ if $(x + 2)$ is one of the factors.

$$\begin{array}{r} \boxed{-2} & 1 & 1 & -4 & -4 \\ & -2 & 2 & 4 \\ \hline & 1 & -1 & -2 & 0 \end{array} \quad \begin{array}{l} x^2 - x - 2 \\ (x - 2)(x + 1) \end{array} \quad (x - 2)(x + 1)(x + 2)$$

3. $15x^3 + 14x^2 - 3x - 2$ if $(x + 1)$ is one of the factors.

$$\begin{array}{r} \boxed{-1} & 15 & 14 & -3 & -2 \\ & -15 & 1 & 2 \\ \hline & 15 & -1 & -2 & 0 \end{array} \quad \begin{array}{l} 15x^2 - x - 2 \\ (3x + 1)(5x - 2) \end{array} \quad (3x + 1)(5x - 2)(x + 1)$$

4. $3x^3 + 13x^2 - 52x + 28$ if $(x + 7)$ is one of the factors.

$$\begin{array}{r} \boxed{-7} & 3 & 13 & -52 & 28 \\ & -21 & 56 & -28 \\ \hline & 3 & -8 & 4 & 0 \end{array} \quad \begin{array}{l} 3x^2 - 8x + 4 \\ (3x - 2)(x - 2) \end{array} \quad (3x - 2)(x - 2)(x + 7)$$

5. $8x^3 - 2x^2 - 41x - 10$ if $(x + 2)$ is one of the factors.

$$\begin{array}{r} \boxed{-2} & 8 & -2 & -41 & -10 \\ & -16 & 36 & 10 \\ \hline & 8 & -18 & -5 & 0 \end{array} \quad \begin{array}{l} 8x^2 - 18x - 5 \\ (4x + 1)(2x - 5) \end{array} \quad (x + 2)(4x + 1)(2x - 5)$$

6. $x^3 - x^2 - 8x + 12$ if $(x + 3)$ is one of the factors.

$$\begin{array}{r} \boxed{-3} & 1 & -1 & -8 & 12 \\ & -3 & 12 & -12 \\ \hline & 1 & -4 & 4 & 0 \end{array} \quad \begin{array}{l} x^2 - 4x + 4 \\ (x - 2)(x - 2) \end{array} \quad (x - 2)^2(x + 3)$$

7. $x^3 - 2x^2 - 7x - 4$ if $(x + 1)$ is one of the factors.

$$\begin{array}{r} \boxed{-1} & 1 & -2 & -7 & -4 \\ & -1 & 3 & 4 \\ \hline & 1 & -3 & -4 & 0 \end{array} \quad \begin{array}{l} x^2 - 3x - 4 \\ (x - 4)(x + 1) \end{array} \quad (x - 4)(x + 1)^2 \quad (x - 4)(x + 1)(x + 1)$$

8. $x^4 + 4x^3 - x^2 - 16x - 12$ if $(x^2 - 4)$ is one of the factors.

$$\begin{array}{r} x^2 + 0x - 4 & \overline{x^4 + 4x^3 - x^2 - 16x - 12} \\ & - x^4 + 0 \quad \cancel{- 4x^2} \\ \hline & 4x^3 + 3x^2 - 16x \\ & - 4x^3 + 0 \quad \cancel{- 16x} \\ \hline & 3x^2 + 0 - 12 \\ & 3x^2 + 0 - 12 \end{array} \quad \begin{array}{l} x^2 + 4x + 3 \\ (x^2 + 4x + 3)(x^2 - 4) \end{array} \quad (x + 3)(x + 1)(x + 2)(x - 2)$$

Factor each completely.

9. $5x^3 + 2x^2 + 10x + 4$
 $x^2(5x+2) + 2(5x+2)$
 $(5x+2)(x^2+2)$

10. $27x^3 + 1$ $(3x+1)(9x^2 - 3x + 1)$

11. $2x^2 - 2x - 60$
 $2(x^2 - x - 30)$
 $2(x - 6)(x + 5)$

12. $x^3 + 11x^2 + 28x$
 $x(x^2 + 11x + 28)$
 $x(x + 4)(x + 7)$

13. $4x^2 + 28x$
 $4x(x + 7)$

14. $x^4 + 2x^2 + 1$
 $(x^2 + 1)(x^2 + 1)$
 $(x^2 + 1)^2$

15. $4x^2 - 25$
 $(2x + 5)(2x - 5)$

16. $16x^2 - 24x + 9$
 $(4x - 3)(4x - 3)$
 $(4x - 3)^2$

17. $12x^3 + 15x^2 + 4x + 5$
 $3x^2(4x + 5) + (4x + 5)$
 $(4x + 5)(3x^2 + 1)$

18. $54 + 250x^3$
 $2(27 + 125x^3)$
 $2(3 + 5x)(9 - 15x + 25x^2)$

19. $7x^2 + 15x + 8$
 $(7x + 8)(x + 1)$

20. $5x^2 - 24x - 5$
 $(5x + 1)(x - 5)$

21. $9x^2 + 23x - 12$
 $(9x - 4)(x + 3)$

22. $10x^2 - 7x + 1$
 $(5x - 1)(2x - 1)$

23. $10x^2 + 63x + 18$
 $(1x + 6)(10x + 3)$

24. $8x^2 - 21x - 9$
 $(1x - 3)(8x + 3)$

25. $3x^2 - 22x - 45$
 $(3x + 5)(x - 9)$

26. $7x^2 - 31x + 30$
 $(7x - 10)(x - 3)$

27. $3x^3 + 3$
 $3(x^3 + 1)$
 $3(x + 1)(x^2 - x + 1)$

28. $6x^2 + 7x - 24$
 $(2x - 3)(3x + 8)$

29. $9x^2 + 21x - 14$

30. $4x^2 - 29x - 24$

DNF

$(4x + 3)(x - 8)$