

Write a polynomial function of least degree that has rational coefficients, a leading coefficient of 1 and the given zeros.

1.  $1, 2, 3$

2.  $-2, 1, 3$

3.  $\sqrt{3}, -\sqrt{3}$

4.  $5i, -5i$

5.  $4, \sqrt{5}, -\sqrt{5}$

6.  $-3, 1, 6$

7.  $2, -2$

8.  $4 + i, 4 - i$

9.  $3 + 2i, 3 - 2i$

10.  $7i, -7i$

Divide using long division.

11.  $5x^4 + 2x^3 - 9x + 12 \div x^2 - 3x + 4$

12.  $x^3 + 11x^2 + 25x - 21 \div x + 7$

Divide using synthetic division.

13.  $2x^4 - 11x^3 + 15x^2 + 6x - 18 \div x - 3$

14.  $x^4 - 6x^3 - 40x + 33 \div x - 7$

Factor completely.

15.  $9y^2 - 64$

16.  $5x^3 + 5x^2 + 30x$

17.  $x^3 + 8y^3$

18.  $5x^4 + 10x^2 - 15$

19.  $2x^3 - 3x^2 + 4x - 6$

20.  $x^3 + 3x^2 - 4x - 12$

21.  $64x^3 - 27y^3$

22.  $x^4 - 13x^2 + 36$

23.  $15x^3 + 14x^2 - 3x - 2$  if  $(x + 1)$  is one of the factors.

24.  $x^3 - x^2 - 8x + 12$  if  $(x + 3)$  is one of the factors.

Solve.

$$25. \quad x^4 - 9x^2 + 14 = 0$$

$$26. \quad 10x^4 - 160 = 0$$

$$27. \quad 6x^2 + 11x - 35 = 0$$

$$28. \quad 12x^2 - 21x - 45 = 0$$

Write the end behavior for the polynomial function.

$$29. \quad g(x) = 2x^3 - 3x + 1$$

$$30. \quad f(x) = -3x^7 + 5x^4 - 2x + 4$$

$$31. \quad h(x) = x^4 - 4x + 2$$

$$32. \quad f(x) = -6x^8 - 25$$

Decide whether the function is a polynomial function. If so, state its degree, type (constant, linear, quadratic, etc.), and leading coefficient.

$$33. \quad f(x) = 78$$

$$34. \quad g(x) = -2x^3 - 2x^2 + 3$$

$$35. \quad g(x) = 4x^2 - x^{-2} + 3$$

$$36. \quad f(x) = -8 + 3x + x^4 - x^2$$

Perform the indicated operation.

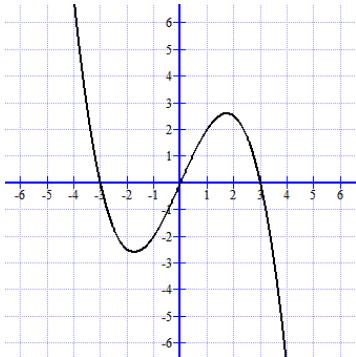
37.  $(x^3 + x^2 - 6) - (2x^2 + 4x - 8)$

38.  $(-3x^2 + 4x - 10) + (x^2 - 9x + 15)$

39. Write a cubic function whose graph passes through the points.

$(3, 0), (-3, 0), (4, 0), (0, 36)$

40. Write a cubic function whose graph is shown.



Simplify.

41.  $\left(\frac{3}{5}\right)^{-2}$

42.  $\left(\frac{2}{3^{-2}}\right)^2$

43.  $(x^4y^{-2})(x^{-3}y^8)$

44.  $(a^2b^{-5})^{-3}$

45.  $(-3c^3d^4e^6)^2$

46.  $\frac{12x^{-3}}{y^4} \cdot \frac{(y^{-2}x^2)^{-2}}{15x^{-2}}$

47.  $\frac{x^3y^7}{x^{-4}y^0}$

48.  $\frac{c^3d^{-2}}{c^5d^{-1}}$