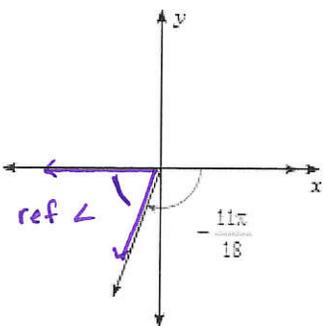
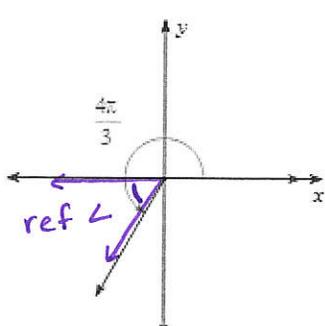
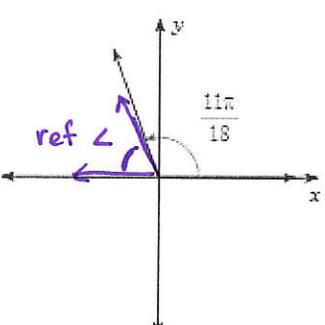
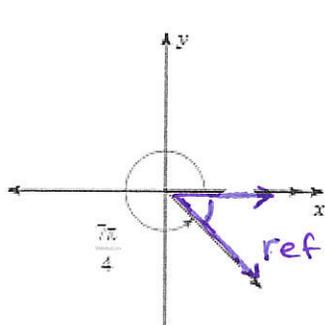
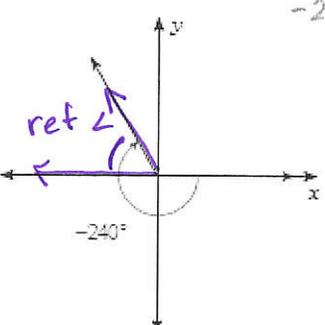
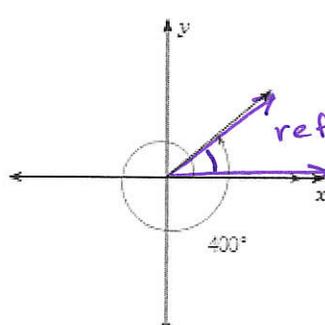
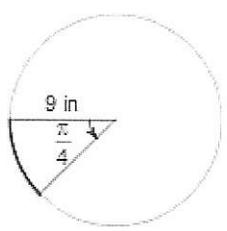
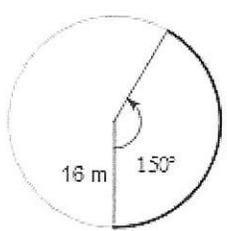


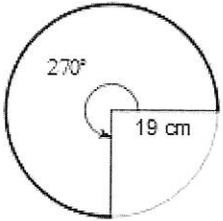
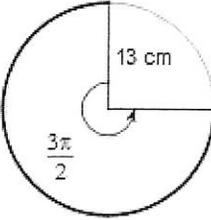
Find the reference angle.

<p>1.</p>  <p><math>180^\circ = \pi</math></p> <p><math>\pi - \frac{11\pi}{18}</math></p> <p><math>\frac{18\pi}{18} - \frac{11\pi}{18} =</math></p> <p><math>\frac{7\pi}{18}</math></p>	<p>2.</p>  <p><math>180^\circ = \pi</math></p> <p><math>\frac{4\pi}{3} - \pi</math></p> <p><math>\frac{4\pi}{3} - \frac{3\pi}{3} =</math></p> <p><math>\frac{\pi}{3}</math></p>
<p>3.</p>  <p><math>\pi - \frac{11\pi}{18}</math></p> <p><math>\frac{18\pi}{18} - \frac{11\pi}{18}</math></p> <p><math>\frac{7\pi}{18}</math></p>	<p>4.</p>  <p><math>2\pi = 360^\circ</math></p> <p><math>2\pi - \frac{7\pi}{4}</math></p> <p><math>\frac{8\pi}{4} - \frac{7\pi}{4} =</math></p> <p><math>\frac{\pi}{4}</math></p>
<p>5.</p>  <p><math>-240^\circ + 180^\circ</math></p> <p><math>60^\circ</math></p>	<p>6.</p>  <p><math>400^\circ - 360^\circ</math></p> <p><math>40^\circ</math></p>

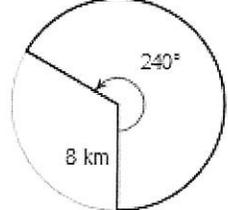
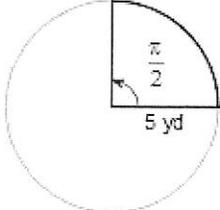
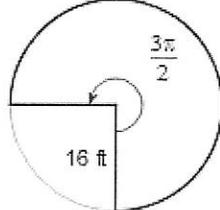
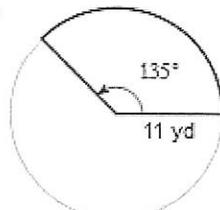
Find the length of each arc.

<p>7.</p>  <p><math>s = r\theta</math></p> <p><math>s = 9(\pi/4)</math></p> <p><math>s = 9\pi/4</math> in</p> <p><math>s \approx 7.07</math></p>	<p>8.</p>  <p><math>s = r\theta</math>    <math>150^\circ (\pi/180^\circ) = \frac{5\pi}{6}</math></p> <p><math>s = 16(5\pi/6) = \frac{40\pi}{3}</math></p> <p><math>s \approx 41.89</math> m</p> <p>or</p> <p><math>s = \frac{150^\circ}{360^\circ} (32\pi) \approx 41.89</math></p>
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Find the length of each arc.

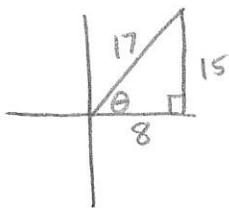
<p>9.</p>  <p><math>S = r\theta \quad \left(\frac{\pi}{180^\circ}\right)(270^\circ)</math></p> <p><math>S = 19(3\pi/2)</math></p> <p><math>S = \frac{57\pi}{2}</math></p> <p><math>S \approx 89.54 \text{ cm}</math></p>	<p>10.</p> <p><math>r = 5 \text{ km}, \theta = \frac{\pi}{3}</math></p> <p><math>S = (5)(\pi/3)</math></p> <p><math>S = \frac{5\pi}{3}</math></p> <p><math>S \approx 5.24 \text{ km}</math></p>
<p>11.</p> <p><math>r = 11 \text{ m}, \theta = 75^\circ</math></p> <p><math>(75^\circ)\left(\frac{\pi}{180^\circ}\right) = 5\pi/12</math></p> <p><math>S = (11)(5\pi/12)</math></p> <p><math>S = \frac{55\pi}{12}</math></p> <p><math>S \approx 14.4 \text{ m}</math></p>	<p>12.</p>  <p><math>S = 13(3\pi/2)</math></p> <p><math>S = 39\pi/2</math></p> <p><math>S \approx 61.26 \text{ cm}</math></p>

Find the area of each sector.

<p>13.</p>  <p><math>A = \frac{1}{2}r^2\theta</math></p> <p><math>A = \frac{1}{2}(8)^2(4\pi/3)</math></p> <p><math>A = \frac{128\pi}{3}</math></p> <p><math>240^\circ\left(\frac{\pi}{180^\circ}\right) = 4\pi/3</math></p> <p><math>A \approx 134.04 \text{ km}^2</math></p>	<p>14.</p> <p><math>r = 12 \text{ m}, \theta = \frac{7\pi}{4}</math></p> <p><math>A = \frac{1}{2}r^2\theta</math></p> <p><math>A = \frac{1}{2}(12)^2(7\pi/4)</math></p> <p><math>A = 126\pi</math></p> <p><math>A \approx 395.84 \text{ m}^2</math></p>
<p>15.</p>  <p><math>A = \frac{1}{2}(5)^2(\pi/2)</math></p> <p><math>A = \frac{25\pi}{4}</math></p> <p><math>A \approx 19.63 \text{ yd}^2</math></p>	<p>16.</p>  <p><math>A = \frac{1}{2}(16)^2\left(\frac{3\pi}{2}\right)</math></p> <p><math>A = 192\pi</math></p> <p><math>A \approx 603.2 \text{ ft}^2</math></p>
<p>17.</p> <p><math>r = 10 \text{ ft}, \theta = 210^\circ</math></p> <p><math>\theta = 210^\circ\left(\frac{\pi}{180^\circ}\right)</math></p> <p><math>\theta = 7\pi/6</math></p> <p><math>A = \frac{1}{2}(10)^2(7\pi/6)</math></p> <p><math>A = \frac{175\pi}{3}</math></p> <p><math>A \approx 183.3 \text{ mi}^2</math></p>	<p>18.</p>  <p><math>A = \frac{1}{2}(11)^2\left(\frac{3\pi}{4}\right)</math></p> <p><math>A = \frac{363\pi}{8}</math></p> <p><math>135^\circ\left(\frac{\pi}{180^\circ}\right) = \frac{3\pi}{4}</math></p> <p><math>A \approx 142.5 \text{ yd}^2</math></p>

Use the given point on the terminal side of an angle  $\theta$  in standard position to evaluate the six trigonometric functions of  $\theta$ .

19. (8, 15)



$$\sin \theta = \frac{15}{17}$$

$$\cos \theta = \frac{8}{17}$$

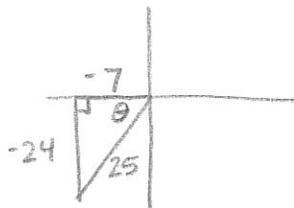
$$\tan \theta = \frac{15}{8}$$

$$\csc \theta = \frac{17}{15}$$

$$\sec \theta = \frac{17}{8}$$

$$\cot \theta = \frac{8}{15}$$

20. (-7, -24)



$$\sin \theta = -\frac{24}{25}$$

$$\cos \theta = -\frac{7}{25}$$

$$\tan \theta = \frac{24}{7}$$

$$\csc \theta = -\frac{25}{24}$$

$$\sec \theta = -\frac{25}{7}$$

$$\cot \theta = \frac{7}{24}$$

Find the value of each. Round your answer to the nearest ten-thousandths.

21.  $\csc 61^\circ$

$$\frac{1}{\sin 61^\circ} \approx 1.1434$$

22.  $\sin 13^\circ \approx .2250$

23.  $\cos 22^\circ \approx .9272$

24.  $\cot 21^\circ$

$$\frac{1}{\tan 21^\circ} \approx 2.6051$$

25.  $\tan \frac{7\pi}{36}$  Change to radian mode

$$\approx .7002$$

26.  $\tan \frac{5\pi}{18}$

$$\approx 1.1918$$

27.  $\cot \frac{5\pi}{36}$

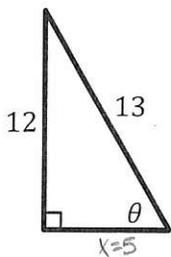
$$\frac{1}{\tan \frac{5\pi}{36}} \approx 2.1445$$

28.  $\cos \frac{5\pi}{18}$

$$\approx .6428$$

Find the value of the trig function indicated.

29.  $\tan \theta =$

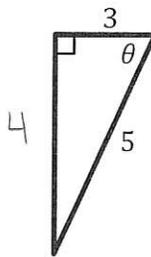


$$\tan \theta = \frac{12}{5}$$

$$x^2 + 12^2 = 13^2$$

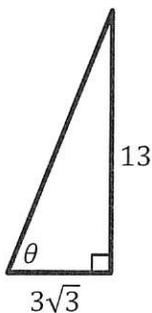
$$x = 5$$

30.  $\cot \theta =$



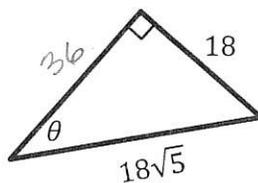
$$\cot \theta = \frac{3}{4}$$

31.  $\cot \theta =$



$$\cot \theta = \frac{3\sqrt{3}}{13}$$

32.  $\tan \theta =$



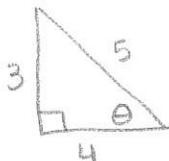
$$\tan \theta = \frac{18}{36}$$

$$x^2 + 18^2 = (18\sqrt{5})^2$$

$$x = 36$$

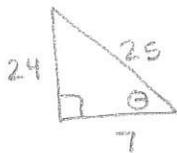
$$\tan \theta = \frac{1}{2}$$

33. Find  $\cos \theta$  if  $\sin \theta = \frac{3}{5}$  opp hyp



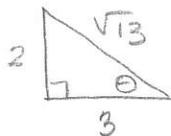
$$\cos \theta = \frac{4}{5}$$

34. Find  $\sec \theta$  if  $\cot \theta = \frac{7}{24}$  adj opp



$$\sec \theta = \frac{25}{7}$$

35. Find  $\cos \theta$  if  $\csc \theta = \frac{\sqrt{13}}{2}$  hyp opp



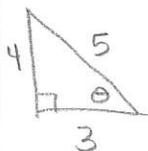
$$\cos \theta = \frac{3}{\sqrt{13}}$$

$$2^2 + x^2 = (\sqrt{13})^2$$

$$x = 3$$

$$\cos \theta = \frac{3\sqrt{13}}{13}$$

36. Find  $\sec \theta$  if  $\sin \theta = \frac{4}{5}$



$$\sec \theta = \frac{5}{3}$$